

BEARs (Spoiler)

Lets begin with a somewhat easier task: given an integer d , we need to find out whether the sheriff can keep the BEARs at least at a distance d from the warehouse. In other words, can the sheriff block streets in such way that the BEARs wouldn't be able to enter any intersection strictly bounded by a square with vertices at $(\pm d, \pm d)$. Let K be the set of intersections within this square (excluding intersections on edges and vertices).

Let A be the set of intersections such that if the BEARs start in an intersection in A they will be able to reach an intersection in K no matter what the sheriff will do. We can express A as the minimal set of intersections such that any intersection S is in set A if at least one of the following holds:

- (1) S is in K ;
- (2) there is a main street segment from S leading to an intersection in A ;
- (3) at least two of the neighbouring intersections are in A .

Note that because of (3), A will always be a rectangle.

We can construct the set A iteratively. Lets begin with $A = K$. Then for every main street that has at least one intersection in A , we extend A so that it would include all intersections in that main street. We do this until there are no main streets to add.

Now, if the intersection (a, b) is in A , the BEARs will reach an intersection in K .

We can now use bisection to find the maximum value of d for which the BEARs won't be able to reach K .

We construct the set A in $O(N^2)$, thus we solve the task in $O(N^2 \log \max\{|A|, |B|\})$.